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# **International economic integration: patterns of catching-up, foreign direct investment and migration flows**

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## ABSTRACT

This paper develops a Schumpeterian model of international specialization and catching-up. In a previous version of the model we looked at the impact on international trade specialization when different patterns of technological catching-up are followed. One of these is a Gerschenkron pattern at the industrial level, where the largest initial gaps in productivity give rise to the fastest relative productivity growth rates. Depending on the productivity, wage and profits dynamic there can be 'comparative advantage switch-overs' in which a catching-up economy turns its competitive advantage towards medium- to high-tech areas. In this paper we follow up the impact of the unit profit or 'rent' patterns on foreign investment and thought that on the speed of technology transfer and hence on differential productivity growth. We show that labour market dynamics, productivity catching-up and investment patterns all combine to determine the evolution of the international division of labour. We point also to the impact on labour demand and wage structures (between skilled and unskilled workers) both in the lead and the catching-up economies. The model thus contributes to the literature on globalization and labour markets.

**Keywords:** international integration, FDI, endogenous productivity growth, catching-up, international specialization, trade and employment, migration

**JEL-Classification:** F15, F16, F21, F22, F43, O41

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# International economic integration: patterns of catching-up, foreign direct investment and migration flows

M. Landesmann and R. Stehrer

## 1 Introduction

This paper builds on a model introduced by Landesmann and Stehrer (2000) and Stehrer (2002). In the present paper we endogenise FDI flows and bring in a number of issues which show how FDI may play an important role in codetermining international specialisation and catching-up patterns. In fact, the causality runs both ways: the nature of catching-up determines the overall quantity and industrial allocation of FDI across branches of a catching-up economy and FDI in turn affects the pattern of catching-up. The previous version of the model focussed on the endogenisation of the dynamics of specialisation in a global economy which depended on the detailed modelling of sectoral patterns of productivity growth as well as wage dynamics in both the (technologically) advanced and the catching-up economies. It could be shown that, adopting a Gerschenkron pattern of catching-up at the sectoral level (i.e. industries with a higher initial productivity gap have a greater scope for productivity growth), can turn the comparative advantage of catching-up economies towards technologically advanced industries, even if the absolute level of productivity of the catching-up economy remains below that of the advanced economy. We spoke in this context of a 'comparative advantage switchover'. The Schumpeterian feature of our model, particularly the emergence of transitory per-unit rents allows an interesting integration of FDI flows into our model. Global investment flows are sensitive towards the emergence of per-unit rents and hence, implicitly, to the productivity- and wage-dynamics of catching up. Using a simple formulation for 'endogenising' productivity growth as a function of FDI flows (representing the impact of FDI on technology transfer) we show that FDI flows in turn impact upon the sectoral patterns of catching-up and hence on the dynamics of comparative advantage.

On the technical side, the integration of FDI into our model reveals a feature of disequilibrium dynamics: the building-up of capacities becomes both demand- and supply-determined. The latter refers to the impact which high unit-rents (Schumpeterian profits) have upon the attractiveness to expand capacities in particular sectors and locations/countries. The utilisation of such capacities is, on the other hand, demand-determined, and hence a function of whether such sectors and locations are able to attract the additional demand required for such utilisation. We shall see that this opens up an additional dynamic where utilisation patterns depend in turn on productivity-wage-price dynamics and a number of price elasticities of demand.

We start in the following with a short verbal account of the main features of the model within which we explore the impact of FDI on the dynamics on international specialisation and catching-up. This is followed by a discussion of the way we specify the determinants and effects of FDI in the model. In sections 2 and 3 we give a formal account of the

structure of the model and in section 4 we explore some qualitative features of the impact of FDI with a number of model simulations.

## 1.1 A short description of the model

The model is designed to present the structural features of international economic integration: The model is multi-sectoral, distinguishing a range of industries and their development, so that structural change can be represented. It formulates dynamics with respect to productivity growth (differentiated across sectors) and wage and price movements, it allows for skill and wage differentiation across workers and it introduces Schumpeterian features in the form of the emergence of transitory unit rents which get eroded over time (through price cost adjustments). The outcome is a trade cum growth model in which transitory dynamics and shifts in steady-states drives changes in international comparative advantage (in a Ricardian sense).

The mechanisms inducing structural change are manifold: on the supply side, it is the uneven evolution of productivity (across sectors) which initiates changes in cost and price structures and hence causes substitution effects in the structures of demand (in final demand and in the sourcing of intermediate inputs). The opening up of price-cost gaps during the transitory dynamics which gives rise to Schumpeterian unit-rents is also the cause of an uneven investment dynamics which is financed by transitory retained earnings. There are two forms of endogenous productivity effects: one linked to output growth (Kaldor-Verdoorn), the other resulting from the investment dynamics (Schumpeter-Arrow). The endogenous productivity effects have further repercussions on the supply-side determinants of structural change. On the demand side, demand functions are specified in a traditional manner with sensitivity to relative prices (substitution effects) and levels of real incomes (Engels effects).

In an international context, it is the relative dynamic of productivity, wages, prices, and unit rents which matters in determining two forms of competitiveness: competitiveness in product markets (resulting from the dynamics of relative unit costs and prices) and competitiveness on capital markets, particularly in the area of attractiveness to FDI (resulting from differential unit rents). In an integrated global economy, the two forms of competitiveness determine the evolution of relative specialisation, trade structures and the global allocation of FDI. The resulting relative output and investment dynamic has further endogenous productivity growth and catching-up effects. Let us now turn to a more explicit discussion of the determinants and effects of FDI in our model.

## 1.2 Endogenising FDI flows:determinants and effects

We shall assume that the allocation of FDI flows is determined by differential per-unit rents<sup>1</sup> which arise in different industrial branches and different international locations. In general, FDI should be forward looking and not be just dependent upon current per-unit

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<sup>1</sup>In a model with circulating capital only, this amounts to the same thing as differential rates of return on invested capital (with wages paid ex ante).

profits, but we shall have to assume this as long as we do not implement a forward looking integral about expected (discounted) flows of returns.

What are the effects of FDI flows? We shall discuss three direct effects: One is a capacity effect, i.e. FDI generates additional capacity, the other is an impact on productivity, i.e. a speeding up of technology transfer, and the third might be an impact on market structure which might affect the price-cost margins.

Let us deal with the capacity effect first: FDI flows will generate additional production capacity of the level determined by the real value of inputs (capital equipment and labour) which can be purchased from these flows. There will be an issue here in relation to the technology and sourcing structure (of inputs) associated with FDI generated production capacity. Another issue concerns the utilisation of these capacities. The model will make a distinction between the build-up of capacity and its utilisation. Actual production levels will be determined by demand, while capacity emergence from profitability of investments which is determined by (expected) per-unit earnings on capital.

In the model there is not an automatic adjustment of supply (the build-up of additional capacities through FDI and home investments) and demand. In phases of adjustments in which additional capacity is generated by FDI inflows there is a potential demand-supply mismatch. The model converges to a long-run equilibrium where prices equal (average) costs plus a (long-run) mark up and supply equals demand. We do not however specify an immediate (and necessarily infinitely fast) price-setting mechanism to equilibrate demand and supply, given capacities. We think that the approach taken here allows us to address real phenomena (problems of adjustment) which are not dealt with in neoclassical (equilibrium spot market) models. This, however, comes at the cost of temporary (supply-demand) imbalances which characterise the model's behaviour during transitory phases.

The next effect is an 'endogenous productivity' effect: We shall assume that FDI can speed up the technology transfer in the catching-up economy but not allow the country to shift the technology frontier itself (the latter is defined by the productivity level of the more advanced economy). This reduces the possibility of a cumulative process where competitiveness may be improved to a level which drives out the advanced economy completely. If only technology transfer is speeded up, there is a limitation of the degree to which a catching-up economy can benefit (technologically) from increased FDI inflows (i.e. it can maximally reach the productivity level of the more advanced economy).

There is also an empirical rationale behind this specification in that MNCs do not set up sites in less developed economies which are technologically superior to the ones in the home base. A real process of technological 'overtaking' could occur if there is a building up of human capital stock and R&D infrastructure superior to that of the technological leader; this could occur as a function of domestic public policy and - under certain circumstances - be the result of the ways how factor markets operate in different economies.

Once FDI affects productivity growth, we shall have the scenario that fast learning in the technologically advanced industries combined with moderate wage increases leads to high per-unit rents in these industries; this makes them attractive for FDI inflows and this speeds up productivity growth further. There will be a limitation in this productivity

growth push in that the Gerschenkron mechanism (advantage of backwardness) can be exhausted and hence at some point productivity growth in spite of FDI inflows will slow down as productivity levels of the more advanced economy are approached. In the long-run we approach a steady-state with equal unit costs in all countries (and with an undefined specialisation structure).

Before this long-run steady-state is reached however, specialisation advantages in the high-tech branches by the catching-up country are enforced by FDI productivity effects. Of course, as always, productivity catching-up is only one side of the story, the other is wage catching-up. And we know that any move in the direction of specialisation towards high tech branches, requires an increased relative demand for skilled workers and hence increases the pressure (given the composition of the labour force) on the wage rates of the skilled workers.

The third and last effect refers to the impact upon market structure: We shall allow FDI to have an impact on the parameter of price-to-cost adjustment so that (even without an impact on endogenous productivity growth) there would also be a direct impact of FDI on international market shares as long as there are disequilibrium price-cost margins. The rationale for this is that FDI flows imply an opening of markets (to new entrants) and thus increase the competitive pressure in domestic markets (leading to a faster price-to-cost adjustment). Of course, it does not always have to work in this direction: There could e.g. be trade (and other entry) barriers so that the foreign investor who 'jumps' over the existing barriers would find a rather protected domestic market and has little incentive to forego a profit margin. If he is a 'contested' new entrant (i.e. no entry barriers for other new entrants), then the pressure to behave competitively will be there, but there might still be high fixed costs to cover in the first phase of entry so that the foreign investor will have to keep the margin to cover the fixed costs (typical situation in endogenous growth models).

## 2 The model

In this section we present the detailed structure of the model, which is used afterwards in simulation studies. The model is based on a paper by Landesmann and Stehrer (2000) and a more extended version by Stehrer (2002). The version of the model presented in this paper brings in the role of FDI as an important mover in the dynamics of catching-up and in the evolution of comparative advantage.

### 2.1 Technology

#### 2.1.1 Input-output matrix

We start with a matrix of technical input coefficients for each country  $c$ , denoted by

$$\mathbf{A}^c = \left( \begin{array}{cccc} \tilde{\mathbf{a}}_{*1}^c & \dots & \tilde{\mathbf{a}}_{*i}^c & \dots & \tilde{\mathbf{a}}_{*N}^c \end{array} \right)$$

where

$$\tilde{\mathbf{a}}_{*i}^c = \left( \begin{array}{cccc} \tilde{a}_{1i}^c & \dots & \tilde{a}_{ji}^c & \dots & \tilde{a}_{ni}^c \end{array} \right)^\top$$

and the typical element  $\tilde{a}_{ji}^c$  denotes a *technical* input coefficient of sector  $i$  in country  $c$ . These technical coefficients are assumed to be stable over time (i.e. determined by technological considerations). The technical coefficients must be distinguished from the demand matrix for intermediate inputs as goods may be purchased from different suppliers; we shall refer to this demand matrix as the 'sourcing matrix'; the elements of that matrix will be price sensitive as we shall allow for substitution (as well as 'home' and 'regional bias') effects. We denote the demand coefficients for intermediate inputs supplied by country  $c$  to country  $r$  as

$$\mathbf{A}^{cr} = \begin{pmatrix} a_{11}^{cr} & \dots & a_{1N}^{cr} \\ \vdots & \ddots & \vdots \\ a_{N1}^{cr} & \dots & a_{NN}^{cr} \end{pmatrix}$$

These demand (or 'sourcing') coefficients have to satisfy the technologically given constraint  $\tilde{a}_{ji}^r = \sum_c a_{ji}^{cr}$ . The overall world sourcing matrix is then given by

$$\mathbf{A} = \begin{pmatrix} \mathbf{A}^{11} & \dots & \mathbf{A}^{1C} \\ \vdots & \ddots & \vdots \\ \mathbf{A}^{C1} & \dots & \mathbf{A}^{CC} \end{pmatrix}$$

The global sourcing matrix  $\mathbf{A}$  is assumed to satisfy the conditions to guarantee economically meaningful solutions.

### 2.1.2 Labour input coefficients

The goods produced require different types of workers denoted by  $z = 1, \dots, Z$ . We denote the vector of labour input coefficients by

$$\mathbf{a}_{ii}^c = (a_{ii,1}^c \quad \dots \quad a_{ii,Z}^c)$$

where  $a_{ii,z}^c$  denotes the labour input coefficient of skill type  $z$  in industry  $i$  in country  $c$ . We do not allow for substitution effects between different types of labour, although we allow for changes in the composition of labour due to technological change (e.g. skill-biased technological change).

Technological progress is introduced through changes in labour input-coefficients as a steady decrease to an exogenous (stationary) level, i.e.

$$\dot{a}_{ii,z}^c = \gamma_{a_{ii,z}}^c (a_{ii,z}^c - \bar{a}_{ii,z}^c)$$

This simple formulation allows both for differences in the rates of productivity growth, firstly, due to initial 'distance' from the stationary state productivity level and, secondly, due to differences in the speed of adjustment (parameter  $\gamma_{a_{ii,z}}^c$ ) to that level. The same distinction will be used later on to differentiate between a 'weak' and a 'strong' Gerschenkron effect when productivity catching-up processes are considered from the point of view of a catching-up economy.

## 2.2 Prices and rents

**Prices** Prices are modeled as adjustment to unit costs

$$\dot{p}_i^c = -\delta_{p,i}^c [p_i^c - (1 + \pi_i^c)c_i^c]$$

where  $c_i^c = \sum_j p_j^c a_{ji}^c + v_i^c$  are the costs of production and  $v_i^c = \sum_z w_{i,z}^c a_{i,z}^c$  denote the unit labour costs in a particular sector  $i$ . We assume that wage rates (by skill-types)  $w_{i,z}^c$  need not be equal across sectors, although we shall assume that wage rates for each particular skill-group tend to equalise in the long run as we shall see below. The parameter  $0 < \delta_{p,i}^c \leq 1$  gives the speed of adjustment of prices to (equilibrium) unit labour costs. There exists a long run mark-up on prices with  $\pi_i^c$  being the mark-up ratio. This assumption leads to equal per unit profitability across sectors in the long run simply through the price-to-cost adjustment mechanism.<sup>23</sup>

**Rents** As there is a constant long-run mark-up ratio on prices  $\pi_i^c$  there are long-run per unit profits  $r_i^c$  defined as

$$r_i^c = \pi_i^c c_i^c$$

As prices do not adjust immediately to unit costs plus a (long-run) mark-up, there arise *transitory rents*  $s_i^c$  depending on the speed of technological progress, the price-to-cost adjustment parameter  $\delta_{p,i}^c$  and the dynamics of wages as we shall see below:

$$s_i^c = p_i^c - (1 + \pi_i^c)c_i^c = p_i^c - c_i^c - \pi_i^c c_i^c = p_i^c - c_i^c - r_i^c$$

## 2.3 Labour market

**Wage rates** Nominal wages are growing or falling for three reasons: First, transitory rents are partly distributed to workers; second, excess supply (demand) of workers in the labour market drives wages up or down; and third, we assume skill-specific wage equalisation across sectors in the long-run. These three factors are formulated as follows:

$$\dot{w}_{i,z}^c = \kappa_{s,i,z}^c \frac{s_i^c}{\sum_z a_{i,z}^c} + \kappa_{u,z}^c u_z^c w_{i,z}^c + \kappa_{w,z}^c \frac{w_{i,z}^c - \bar{w}_z^c}{w_{i,z}^c} \quad \text{with} \quad \kappa_{s,i,z}^c = \kappa_{s,i}^c \frac{w_{i,z}^c}{\sum_z w_{i,z}^c}$$

$0 \leq \kappa_{s,i}^c \leq 1$  is the proportion of per unit (transitory) rents  $s_i^c$  paid to workers (bargaining coefficient). The specification of the first term on the rhs of the wage equation implies that wage rates of different types of workers are absorbing a certain proportion of sector-specific rents (the latter are defined per unit of output). This means that wage rates can (temporarily) be different across sectors and skill-groups as rents are, in the first instance, distributed only to workers in the respective sector where the rents arise.

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<sup>2</sup>In addition, there will be other mechanisms at work in the model which lead to long-run equilibration: one is the pressure on wage rates when a sector has above-average unit-rents; the other is the allocation (see below) of additional investment flows into a sector with high per-unit rents which increases labour demand and thus provides another mechanism for wage (and hence unit cost) pressure in that sector.

<sup>3</sup>At this stage we do not introduce exchange rate dynamics and assume the exchange rates to be constant. This means that all nominal values are expressed in a particular currency.

The second term on the rhs of the wage dynamics equation reflects the impact of unemployment on the dynamics of the wage rates ( $\kappa_{u,z}^c \leq 0$ ). The unemployment rate is defined as

$$u_z^c = \frac{h_z^c - \sum_i a_{li,z}^c q_i^c}{h_z^c} = \frac{h_z^c - \sum_i l_{i,z}^c}{h_z^c}$$

where  $h_z^c$  and  $l_z^c$  denote labour supply and demand, respectively.

Third, there is an impact on the wage dynamics if wage rates (for the same skill-type of worker) differ across sectors. This reflects the common assumption that wage rates get equalised across sectors because of labour mobility. The (weighted) average wage rate (across sectors) is defined as  $\bar{w}_z^c = \frac{\sum_i l_{i,z}^c w_{i,z}^c}{\sum_i l_{i,z}^c}$ . If the average wage  $\bar{w}_z^c$  is higher than the sectorial wage  $w_{i,z}^c$  the wage in sector  $i$  will rise, in the other case fall. This term works across all sectors. Thus in the formulation used in the simulations, there are two sector specific terms and one economy wide term having an influence on wage rates in each sector. Skill-specific wage differentiation can occur across sectors in the short run, but wage rates are equalised for the same skill group across sectors in the long run.

**Labour supply** Skill-specific labour supply  $h_z^c$  is assumed to adjust to labour demand according to

$$\dot{h}_z^c = \delta_{h_z^c}^c (l_z^c - h_z^c)$$

where

$$\delta_{h_z^c}^c = \begin{cases} \delta_{h_z^c, IN} > 0 & \text{for } h_z^c > l_z^c \\ \delta_{h_z^c, OUT} \geq 0 & \text{for } h_z^c \leq l_z^c \end{cases}$$

This formulation implies that labour supply adjusts to labour demand if there is excess demand or excess supply of labour; adjustment occurs at different rates, however. In the first case workers are entering the labour market, in the second case workers leave the labour market in case of unemployment, so that high unemployment leads to a falling participation rate.<sup>4</sup>

In the case of an exogenous inflow (or an exogenous constant growth rate) of workers the labour supply equation is

$$\dot{h}_z^c = \delta_{h_z^c}^c (l_z^c - h_z^c) + \gamma_z^c h_z^c$$

which may reflect human capital policies of different countries. In equilibrium with no technical progress in which the economy is growing at a constant rate  $\gamma_q$  the growth rate of each type of labour must be  $\gamma_z^c = \gamma_q$ . (Of course, the maximum of the work force cannot exceed the stock of this skill type in the population times a long-term participation rate.)

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<sup>4</sup>We do not, at this stage, make the labour supply a function of the real wage - contrary to a typical neo-classical formulation - but a function of the excess-demand for labour, as we think that this mechanism has been shown to be empirically more relevant than the neoclassical mechanism; see e.g. Elmeskov and Pichelmann (1993).

## 3 International economic linkages

### 3.1 Quantities: Demand Side

Following on from the discussion of the price system, the quantity system must be specified. Demand for goods consists of three different components which can be summarized in the following demand equation:

$$q_i^c = \sum_{r,j} a_{ij}^{cr} q_j^r + j_i^c + f_i^c \quad (3.1)$$

The first term is demand for intermediate goods used in production, the second term is (net) investment demand (financed - by assumption - out of profit and rent income) and the third term reflects consumption demand (at this stage assumed to come from workers' incomes).  $j_i^c$  and  $f_i^c$  therefore denote investment and consumption demand respectively for good  $i$ . We discuss each of these items in turn.

#### 3.1.1 Demand for intermediate inputs and the 'global sourcing' matrix

The quantity of intermediate inputs to be purchased in one period of production is  $\mathbf{a}_{*j}^{*r} q_j^r$ ; its nominal value is  $\mathbf{p}^\top \mathbf{a}_{*j}^{*r} q_j^r$ . These intermediate inputs can be purchased from countries  $c$  and hence the nominal share (of total outlays on intermediate goods) spent by a sector  $j$  located in country  $r$  on an intermediate good  $i$  from country  $c$  is given by

$$\beta_{A,ij}^{cr} = \frac{p_i^c a_{ij}^{cr}}{\mathbf{p}^\top \mathbf{a}_{*j}^{*r}}$$

where the (sourcing) coefficients  $a_{ij}^{cr}$  are momentarily given, but are themselves dependent on prices and may thus vary over time. The constraint is given by  $\sum_c a_{ij}^{cr} = \tilde{a}_{ji}^r$ , i.e. the sourcing coefficients of intermediate inputs must sum up to  $\tilde{a}_{ji}^r$ , the technical input coefficient for input  $j$  in sector  $i$  of country  $r$  (see also section 2.1 above).

We apply the following modelling strategy: First, we calculate the expenditure shares for intermediate inputs which sector  $i$  of country  $r$  spends on goods  $j$  from country  $c$  where we use the following CES specification:

$$\zeta_{ij}^{cr} = (p_i^c)^{1-\sigma_{\zeta,ij}^r} (\varrho_{\zeta,ij}^{cr})^{\sigma_{\zeta,ij}^r} \left( \sum_s (p_k^s)^{1-\sigma_{\zeta,ij}^r} (\varrho_{\zeta,ij}^{sr})^{\sigma_{\zeta,ij}^r} \right)^{-1}$$

where  $\sigma_{\zeta,ij}^r$  denotes the elasticity of substitution and  $\varrho_{\zeta,ij}^{cr}$  is a parameter reflecting a 'suppliers bias' (it can be used e.g. to include a 'home bias' or a 'regionalist bias' effect). Whereas  $\sigma_{\zeta,ij}^r$  is the same across (supplier) countries, the weighting parameter  $\varrho_{\zeta,ij}^{cr}$  gives weights to different countries  $c$  which may differ for sectors  $i$  and  $j$ . This formulation satisfies the condition that  $\sum_c \zeta_{ij}^{cr} = 1$ . Setting  $a_{ij}^{cr} = \zeta_{ij}^{cr} \tilde{a}_{ij}^r$  gives the coefficients of the  $\mathbf{A}$  matrix which have to satisfy

$$\sum_c \zeta_{ij}^{cr} \tilde{a}_{ij}^r = \sum_c a_{ij}^{cr} = \tilde{a}_{ij}^r$$

These coefficients give the structure of purchases of intermediate input goods across countries and sectors. In fact, this defines the 'global sourcing matrix'  $\mathbf{A}$  introduced in subsection 2.1 above.

The second step is to calculate the share of the nominal value spent on goods  $k$ . Given the expenditure structures (as we have already determined the sourcing coefficients  $a_{ij}^{cr}$ ) this is determined by

$$\frac{1}{p_i^c} \beta_{A,ij}^{cr} \mathbf{p}^\top \mathbf{a}_{*j}^{*r} q_j^r = \frac{1}{p_i^c} \frac{p_i^c a_{ij}^{cr}}{\mathbf{p}^\top \mathbf{a}_{*j}^{*r}} \mathbf{p}^\top \mathbf{a}_{*j}^{*r} q_j^r = a_{ij}^{cr} q_j^r$$

which refers to demand for good  $i$  in country  $c$  bought by sector  $j$  in country  $r$  which produces  $q_j^r$ .

This formulation allows for substitution across countries when buying intermediate inputs. Please note that this implies that a higher physical amount of intermediate inputs can be purchased as expenditures are allocated more efficiently over countries. Or, alternatively, the same bundle of technologically determined inputs can be purchased at lower costs as expenditures are allocated more efficiently over countries. Positive values for the 'suppliers bias' terms  $\varrho_{\zeta,ij}^{cr}$  thus imply - from the cost side - efficiency losses.

Summing up over countries  $r$  and sectors  $j$  gives the total demand for intermediate inputs in sector  $i$  of country  $c$ :

$$\sum_{r,j} a_{ij}^{cr} q_j^r$$

which is the first component in the demand equation (3.1).

### 3.1.2 Investment demand

Next we specify how income out of retained earnings is spent. We assume that per unit profits and rents which are not distributed to workers, i.e.  $m_k^s = ((1 - \kappa_{s,k}^s) s_k^s + r_k^s)$  are entirely used for investment. Total rents plus profits in nominal terms in the economy  $s$  and sector  $i$  are then given by

$$m_k^s q_k^s = ((1 - \kappa_{s,k}^s) s_k^s + r_k^s) q_k^s$$

In an integrated economy investors have to make two decisions: First, in which country and sector to invest, and second in which country to buy the goods for investment. These questions are guided by different considerations: The first one is motivated by relative per unit rents (and profits), the second by relative prices for purchases of investment goods.

Let us adress the first question. It is reasonable to assume that investments are made in sectors and countries with relatively higher (expected) per unit rents. Second, there are also sector specific investment patterns, i.e. profits made in a sector  $i$  are more likely to be invested in a sector which is 'closer' in terms of sector-specific knowledge (of its technology, its markets, types of industrial relations, etc.). To account for these considerations we assume the following specification. A specific sector  $k$  in country  $s$  invests in sector  $j$  of

country  $r$  the share  $\nu_{kj}^{sr}$  of total retained earnings:

$$\nu_{kj}^{sr} = \begin{cases} (m_j^r)^{\sigma_{\nu,k}^s - 1} (\varrho_{\nu,kj}^{sr})^{\sigma_{\nu,k}^s} \left( \sum_{t,l} (m_l^t)^{\sigma_{\nu,k}^s - 1} (\varrho_{\nu,kl}^{st})^{\sigma_{\nu,k}^s} \right)^{-1} & \text{for } m_l^t > 0 \\ 0 & \text{for } m_l^t \leq 0 \end{cases}$$

which again results from a CES specification.<sup>5</sup> Summing up over all sectors  $k$  in country  $s$  gives the investment of country  $s$  in sector  $j$  of country  $r$   $\sum_k \nu_{kj}^{sr} m_k^s q_k^s$ . Further summing up over countries  $s$  gives total investment in country  $r$  in sector  $j$ :

$$\sum_{s,k} \nu_{kj}^{sr} m_k^s q_k^s$$

Second, one has to specify the country where the goods for investment of country  $c$  in country  $s$  are purchased. This is in general driven by cost considerations and thus by relative prices. We denote the shares by  $\zeta_{ij}^{cr}$ . Again, there are various possibilities: the pattern for purchasing goods may, first, be the same as in the country in which the investment takes place (country  $r$  above) or, second, be the same as that of the investing country (country  $s$  above). The first possibility is more plausible as the investments are made in plants operating in country  $r$ . There can be arguments in favour for the second alternative, e.g. if a multinational keeps its structure of suppliers. But even in this case, one would consider this a transitory phenomenon, as increasingly the sourcing structure might move towards the new location. In the simulations reported below, we shall restrict ourselves to the first possibility.<sup>6</sup> These two possibilities result in different demand patterns.<sup>7</sup>

In the first case the nominal sum invested from sector  $k$  in country  $s$  in sector  $j$  of country  $r$  is allocated over goods  $i$  as does sector  $j$  in the receiving country  $r$ , i.e.

$$\zeta_{ij}^{cr} = \xi_{ij}^{cr}$$

The sourcing coefficients are then  $\xi_{ij}^{cr} \tilde{a}_{ij}^r = a_{ij}^{cr}$ , i.e. the same sourcing coefficients apply as for the intermediate inputs. However, the invested sum in a specific sector has to be

<sup>5</sup>Specifically we set  $m_l^t = 0$  if  $m_l^t < 0$  when calculating the shares  $\nu_{kj}^{sr}$ .

<sup>6</sup>The sourcing structure of a country may change however due to the inflow of foreign direct investment.

<sup>7</sup>In the second case the nominal sum invested from sector  $k$  in country  $s$  in sector  $j$  of country  $r$  is allocated over goods  $i$  as does sector  $j$  in country  $s$ , i.e.

$$\zeta_{ij}^{cs} = \xi_{ij}^{cs}$$

This results in sourcing coefficients  $\xi_{ij}^{cs} \tilde{a}_{ij}^s = a_{ij}^{cs}$ , which results in a demand pattern given by  $\beta_{ij}^{cs} = \frac{p_i^c a_{ij}^{cr}}{\mathbf{p}^c \mathbf{a}_{*j}^{sr}}$ . Summing up over countries  $r$  and sectors  $j$  gives demand for investment goods in sector  $i$  of country  $c$ :

$$j_i^c = \frac{1}{p_i^c} \sum_{j,r} \beta_{ij}^{cs} \sum_{s,k} \nu_{kj}^{sr} m_k^s q_k^s$$

In this case the technology (input coefficients) of the investing country  $s$  would apply in country  $r$ , however. Thus a mixture of techniques would be operated in country  $r$ . Although this is an interesting research task for the future we stick to the first case.

allocated across components for intermediate inputs and demand for workers. Analogously to above the invested sum has to be allocated according to

$$\beta_{j,ij}^{cr} = \frac{p_i^c a_{ij}^{cr}}{\mathbf{p}^\top \mathbf{a}_{*j}^{*r} + v_j^r} \quad \text{and} \quad \beta_{l,j}^r = \frac{w_{j,z}^r a_{l,jz}^r}{\mathbf{p}^\top \mathbf{a}_{*j}^{*r} + v_j^r}$$

where the first term refers to allocation of nominal investment across intermediate inputs and the second term across skill types of workers. In this case demand in country  $c$  is given by

$$j_i^c = \frac{1}{p_i^c} \sum_{j,r} \beta_{j,ij}^{cr} \sum_{s,k} v_{kj}^{sr} m_k^s q_k^s$$

This is the second component in the demand equation (3.1).

### 3.1.3 Consumption demand

For demand on consumption goods we assume in this paper a Cobb-Douglas utility function  $U^c = \sum_{i,r} (q_i^r)^{\alpha_i^{rc}}$  from which the corresponding demand functions can be derived. Specifically we thus assume that the utility function is the same for different skill types of workers and assume homothetic preferences. The corresponding demand function of consumption good of country  $r$  in country  $c$  is given by  $\sum_{j,z} \alpha_i^{cr} \frac{w_{j,z}^r l_{j,z}^r}{p_i^c}$ . Summing up over all countries  $r$  gives consumption demand for good  $j$  in country  $c$ :

$$f_i^c = \sum_{r,j,z} \alpha_i^{cr} \frac{w_{j,z}^r a_{l,jz}^r}{p_i^c} q_j^r$$

which is the third term in the demand equation (3.1).

## 3.2 Demand driven growth

### 3.2.1 Balanced growth

For discussing balanced growth we use a result derived in that the allocation of the nominal sum of retained earnings must satisfy the following condition as similarly shown in Stehrer (2002):

$$v_i^s = \frac{\mathbf{p}^\top \mathbf{a}_{*i}^{*s} q_i^s}{(\mathbf{p}^\top \mathbf{A} \mathbf{q} + \mathbf{v}) \mathbf{q}}$$

which assumes that investment behaviour is the same for all industries and countries. Inserting in the expression for the physical increase in capacities gives

$$\begin{aligned} \frac{1}{p_k^r} \frac{p_k^r a_{ki}^{rs}}{\mathbf{p}^\top \mathbf{a}_{*i}^{*s} + v_i^s} \sum_{c,j} v_{ji}^{cs} m_j^c q_j^c &= \frac{a_{ki}^{rs}}{\mathbf{p}^\top \mathbf{a}_{*i}^{*s} + v_i^s} \frac{(\mathbf{p}^\top \mathbf{a}_{*i}^{*s} + v_i^s) q_i^s}{(\mathbf{p}^\top \mathbf{A} + \mathbf{v}^\top) \mathbf{q}} \sum_{c,j} m_j^c q_j^c \\ &= \frac{\mathbf{m}^\top \mathbf{q}}{(\mathbf{p}^\top \mathbf{A} + \mathbf{v}^\top) \mathbf{q}} a_{ki}^{rs} q_i^s. \end{aligned}$$

Dividing by the existing stock of intermediate inputs  $a_{ki}^{rs}q_i^s$  gives the growth rate of capacities

$$g_i^s = \frac{\mathbf{m}^\top \mathbf{q}}{(\mathbf{p}^\top \mathbf{A} + \mathbf{v}^\top) \mathbf{q}}$$

Note that this growth rate is equal for all sectors and countries as it is just the ratio of the sum of retained earnings and the nominal value of the intermediate inputs, i.e.  $g_i^s = g$  for all  $i, s$ . Analogously one can show that demand for workers (and thus capacities in labour) are growing at the same rate.<sup>8</sup> The dynamics of the output can then be model by

$$\dot{\mathbf{q}} = (\mathbf{I} - \mathbf{A})^{-1}(\mathbf{D}_j + \mathbf{D}_f)\mathbf{q} - \mathbf{q}$$

where  $\mathbf{D}_j$  denotes a matrix with typical element  $\frac{1}{p_i^t} \sum_{j,r} \beta_{lj}^{tr} \nu_{kj}^{sr} m_k^s q_k^s$  and  $\mathbf{D}_f$  denotes a matrix with typical element  $\sum_z \alpha_l^{tr} \frac{w_{j,z}^r a_{j,z}^r q_j^r}{p_i^t}$ . One can show easily that at the balanced growth path the term  $\mathbf{D}_j \mathbf{q}$  collapses to  $g \mathbf{A} \mathbf{q}$ .<sup>9</sup> Further one can show that there exists a solution to the homogenous system of equations and thus supply equals demand (see Stehrer, 2002):

$$\mathbf{q} = \mathbf{A} \mathbf{q} + \mathbf{j} + \mathbf{f}.$$

As  $(\mathbf{D}_j + \mathbf{D}_f)\mathbf{q} = (\mathbf{I} - \mathbf{A})\mathbf{q}$  is satisfied in equilibrium the dynamic model is

$$\dot{\mathbf{q}} = g \mathbf{q}.$$

Further it is satisfied that

$$\mathbf{q} + \dot{\mathbf{q}} = (1 + g)\mathbf{q} = \mathbf{A}^{-1}(g \mathbf{A} \mathbf{q} + \mathbf{A} \mathbf{q})$$

which means that the output can be produced with the available intermediate inputs  $\mathbf{A} \mathbf{q}$  and the goods demanded for investment. At each point in time  $\mathbf{j}$  and  $\mathbf{f}$  is demanded which implies that  $(\mathbf{I} - \mathbf{A})^{-1}(\mathbf{j} + \mathbf{f})$  should be available as intermediate inputs. As however  $\mathbf{j}$  is not consumed, this investment is additionally available for production and thus allows for a growing economy.

The stock of intermediate inputs available at the beginning of the production period is thus augmented by the investments. This allows the economy to grow at the rate  $g$  without constraint on the supply side of goods as at each point in time  $g \mathbf{A} \mathbf{q}$  is added to capacities. The demand side is satisfied by consumption demand from either a growing

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<sup>8</sup>Further one can show that under the assumption of an equal profit rate  $\pi$  in all sectors and countries and in the case that all sectors only investing in their own capacities the growth rate is  $g = \pi$ .

<sup>9</sup>In this case the model collapses to a simple dynamic input-output model. In discrete time the system is written as

$$\begin{aligned} q_{t+1} &= (I - (1 + g)A)^{-1}(f_t)(1 + g) \\ &= (I - A)^{-1}(gAq_t + f_t) \\ &= (I - A)^{-1}(D_j + D_f)q_t \end{aligned}$$

Subtracting  $q_t$  from both sides and taking the limits yields the formulation above.

work force and/or - if labour productivity increases - from consumption spending from growing earnings (of workers and capitalists) and the growing volume of retained profits spent on investment goods.

### 3.2.2 Supply side: capacity effects and transitory disequilibria

In the previous section we discussed the demand side of the system. In this section we analyse the supply side of the system with respect to interpretation in disequilibrium.

**Capacity effects** The capacity effect takes place in country  $r$ , i.e. the receiving country (although the demand effect will also be felt in other economies where intermediate goods are also purchased.) We shall look at this from the viewpoint of country  $r$  as the receiving country and sector  $j$  as the sector in which investments are being made. What matters is that the capacities of sector  $j$  are expanding as a result of the allocation of FDI in the sector which in turn depends on the attractiveness of that sector as a destination of rents and profits made globally. The relative attractiveness of different destinations have been specified before through the 'share' coefficients  $\nu_{kj}^{sr}$ . The rates at which capacities are expanding in these sectors can be determined by calculating the physical purchases (of equipment goods) which can be bought with a particular (nominal) FDI allocation of investments. This in turn depends on the sourcing structure discussed earlier.

Hence, in the first place, the nominal sum which is invested (out of global profits and rents) in sector  $j$  of country  $r$  is given by  $\sum_{s,k} \nu_{kj}^{sr} m_k^s q_k^s$ . The physical increase in capacities is made up of the set of capital goods  $k = 1, \dots, n$ . Under the assumptions above (i.e. the investor faces the same global sourcing coefficients as the domestic producers and thus the coefficients  $\beta_{ij}^{cr}$  are equal for both types of investors) the increase in capacity of the component  $i$  in country  $c$  of a sector  $k$  in country  $r$  derived from additional investment can be calculated as

$$\frac{1}{p_i^c} \beta_{ij,ij}^{cr} \sum_{s,k} \nu_{kj}^{sr} m_k^s q_k^s.$$

Inserting for  $\beta_{ij}^{cr}$ , summing up over all countries  $c$  and dividing by the existing 'stock' of intermediate inputs gives the growth rate of sector  $j$ :

$$g_j^r = \frac{1}{\tilde{a}_{ij}^r q_j^r} \frac{\sum_{s,k} \nu_{kj}^{sr} m_k^s q_k^s}{\mathbf{p}^\top \mathbf{a}_{*j}^{*r}} \tilde{a}_{ij}^r = \frac{\sum_{s,k} \nu_{kj}^{sr} m_k^s q_k^s}{\mathbf{p}^\top \mathbf{a}_{*j}^{*r} q_j^r}.$$

Analogously one can show that demand for labour is growing also at this rate. Thus the derivation of the growth rate guarantees that the increase in capacities (intermediates and labour) would be proportional in all equipment goods  $i$  and for all skill types of workers. Hence, the capacity effect in equipment good  $i$  is equivalent to the overall capacity increase in sector  $j$ . But still capacity in the particular sectors may grow at different rates. Further the two results above show that switching from one supplier country to another would not change the growth rate if both suppliers have the same price. However, switching to a cheaper supplier results in a higher growth rate as more goods can be purchased.

Under the assumption that each sector expands at rate  $g_j^r$  which guarantees full utilisation of capacities labour demand in this sector (at given labour input coefficients) is growing at rate  $g_j^r$  as well. Demand out of workers income spreads over to other sectors and countries via the demand formula given above. Further demand out of rents is growing also at rate  $g_j^r$  which spreads over to other sectors via the allocation of rents for investment and demand out of these flows. The dynamics of the economy is then given by

$$\dot{\mathbf{q}} = (\mathbf{I} - \mathbf{A})^{-1}(\mathbf{D}_j + \mathbf{D}_f)(\mathbf{I} + \mathbf{G})\mathbf{q} - \mathbf{q}$$

where  $\mathbf{D}_j$  denotes a matrix with typical element  $\frac{1}{p_i^t} \sum_{j,r} \beta_{lj}^{tr} \nu_{kj}^{sr} m_k^s q_k^s$  and  $\mathbf{D}_f$  denotes a matrix with typical element  $\sum_z \alpha_l^{tr} \frac{w_{i,z}^r a_{j,z}^r q_j^r}{p_i^c}$ .  $\mathbf{G}$  denotes a diagonal matrix with the sector specific growth rates  $g_j^r$  at the diagonal. Note that for equal growth rates this equation collapses to the dynamic equation for the balanced growth path discussed above.

**Disequilibrium interpretations** Apart from the balanced growth path equilibrium relations are violated. Especially there may arise a capacity-demand mismatch, as the two sides are determined by rather different variables. Thus there may arise excess capacities due to shifts in consumption demand, investment demand or changes in the sourcing matrix. In the case of excess supply being higher than demand for a particular good one could either assume that the goods vanish or that the short-term productivity of the sector decreases or that there is some underutilisation of capacities. On the other hand in the case of excess demand one could either assume that the productivity of this sector increases or that capacities get stretched which allows us to focus on the long-term behaviour of our model rather than to focus on the detailed adjustment to short-term imbalances. Further, as we formulate our analysis in continuous time and, given the (numerical) assumptions in our simulations regarding the adjustment processes, the arising imbalances are negligible.

We interpret the dynamics of the output system in the following manner. As we have seen above the general growth path differs from the balanced growth situation only as the common growth rate is replaced with sector and country specific growth rates  $g_i^c$ . In fact, this gives the 'capacity' output path which would be equal to actual output if consumption and investment demand would also grow at this rate. However, as the latter are driven mainly by expenditure structures which are sensitive to relative prices and relative unit rents in a global economy this is not satisfied in general. Specifically we assume that if this is not satisfied productivity of the system adjusts in a way that actual output is equal to demand; i.e. demand is satisfied in at each point in time via (small and short-term) productivity fluctuations. This does not rule out that there can be a path of overinvestment or underinvestment in particular sectors until the system reaches a steady state. For the moment, we take recourse to the 'productivity assumption' (or stretching of intermediate inputs) which requires a certain flexibility of the productive system to deal with a mismatch between capacity output and demand.

Before coming to the discussion of catching-up patterns and the impact which FDI has on the speed of technology transfer, we still introduce the price side.

### 3.3 International price convergence in the long-run

The last effect of international (market) integration we wish to introduce into our model is the long run tendency of the prices of the same type of goods to converge to the same (weighted) average price ('law of one price'). In the following we assume an exogenous trend for price equalisation. This alters the system of differential equations for prices to

$$\dot{p}_i^c = \delta_{p_i}^c [p_i^c - (1 + \pi)c_i^c] + \delta_{\bar{p}_i}^c \frac{p_i^c - \bar{p}_i}{p_i^c} \quad (3.2)$$

where  $\bar{p}_i = \frac{\sum_r q_i^r p_i^r}{\sum_r q_i^r}$  is a weighted average of the prices in the world market.

### 3.4 International convergence patterns: strong and weak Gerschenkron effects and the impact of FDI on technology transfer

Another much discussed aspect of the linkages which emerge from international economic integration is that countries can learn from each other, i.e. that there are 'knowledge spillovers'. This greatly facilitates the catching-up of technologically backward countries with more advanced countries.

#### 3.4.1 Exogenous catching-up

The simplest modelling strategy, which will be used in this paper, is that countries are catching-up with the leading country (or the technology frontier). Different paths of catching-up processes were investigated in Landesmann and Stehrer (2001) and this discussion will not be repeated here. In the simulations below we assume that a (technologically) lagging country will experience higher rates of productivity growth in those industries which start off with a higher initial productivity gap relative to the leader (this amounts to an application of Gerschenkron's famous thesis of the 'advantage of backwardness' at the industrial level; see also Landesmann and Stehrer (2001) for a theoretical discussion and empirical analysis of this use of the Gerschenkron hypothesis). The specific equations for the catching-up processes are similar to the closed economy case:

$$\dot{a}_{li,z}^c = \gamma_{a_{li,z}}^c (a_{li,z}^c - \bar{a}_{li,z}^L) \quad (3.3)$$

where  $\bar{a}_{li}^L$  denotes the labour input coefficient of the productivity leader (i.e. associated with the global technology frontier)

We distinguish two cases: The 'weak' Gerschenkron effect means that catching-up for the industries takes place at the same rate of convergence, i.e. the convergence parameter is equal across industries. This does not mean however that productivity growth is equal. The 'strong' Gerschenkron effect means that the convergence parameter is higher in one or a subset of industries. As we shall show below if the industries with the higher initial gap show a 'strong' Gerschenkron pattern there may a 'comparative advantage switchover' can take place in the course of catching up.

### 3.4.2 Endogenous catching-up

In a more sophisticated setting, the speed of catching-up could also depend on various proxies of 'social or technological capabilities' in the catching-up economy (this approach is associated with the arguments put forward in Abramovitz (1986); a formalisation and a partial test of this hypothesis is provided in Verspagen (1992)). Proxies for such capabilities (i.e. reflecting the ability of a catching-up economy to absorb and utilise more advanced technology) could be the country-wide or industry-specific skill-structure, exogenously specified learning parameters, the structure and volume of imports and exports (reflecting the embodied part of technology transfer, particularly with respect to imports of capital goods and the incentive effects on technology up-grading which a high export orientation provides, particularly towards high-income markets) and, finally but very importantly, the intensity of flows of foreign direct investments, i.e. FDI. This last point will be introduced in this version of the model by assuming that the speed of technology appropriation  $\gamma_{a_{i,z}}^c$  is a function of FDI inflows.

Thus, we endogenise productivity growth as a function of inward FDI flows. We normalise the effect of FDI by using the physical inflow of foreign direct investment in country  $c$  and sector  $i$  relative to the capacities:

$$FDI_{real,i}^c = \left( \frac{1}{p_k^r} \beta_{ki}^{rc} \sum_{s,j} \nu_{ji}^{sc} m_j^s q_j^s \right) / a_{ki}^{rc} q_i^c$$

Inserting for  $\beta_{ki}^{rc} = \frac{p_k^r a_{ki}^{rc}}{\mathbf{p}^\top \mathbf{a}_{*i}^{rc}}$  gives

$$FDI_{real,i}^c = \frac{\sum_{s,j} \nu_{ji}^{sc} m_j^s q_j^s}{\mathbf{p}^\top \mathbf{a}_{*i}^{rc} q_i^c} \quad \text{for } s \neq c$$

which collapses to a nominal ratio. The specific formulation used in the simulations is

$$\dot{a}_{i,z}^c = (\gamma_{a_{i,z}}^c + \gamma_{FDI,i,z}^c FDI_{real,i}^c) (a_{i,z}^c - \bar{a}_{i,z}^L) \quad (3.4)$$

### 3.5 Migration (and commuting)

A third path of international integration is via migration of workers. Given the set up of the model this can be introduced via the labour supply equations given above.

Generally, there are two important variables for migration: The first is the differential in real wage rates (for a given skill group or even skill/industry specific) and the differential in unemployment rates (again for a particular skill group) between two countries. Third, one has to take into account that the migration potential in each country may differ across skill groups. For migrants we have to determine to which country the people want to move to (or stay); we assume the relative attractiveness of different (destination) locations  $s$  from a host location  $c$  to be expressed by shares  $\theta_z^{sc}$ . Then the resulting flows determine the changes in the labour supplies (by skill type) in the different locations accordingly to

$$\dot{h}_z^c = \delta_{h_z^c}^c (l_z^c - h_z^c) + \sum_s \theta_z^{sc} h_z^s - \sum_s \theta_z^{cs} h_z^c$$

The shares  $\theta_z^{cs}$  are assumed to be determined by a CES function:

$$\theta_z^{rc} = \lambda_z^c (\tilde{w}_z^{rc})^{1-\sigma_{(\theta)z}^c} (\varrho_{(\theta)z}^{rc})^{\sigma_{(\theta)z}^c} \left( \sum_s (\tilde{w}_z^{sc})^{1-\sigma_{(\theta)z}^{sc}} (\varrho_{(\theta)z}^{sc})^{\sigma_{(\theta)z}^{sc}} \right)^{-1} + (1 - \lambda_z^c) (\tilde{u}_z^{rc})^{1-\sigma_{(\theta)z}^c} (\varrho_{(\theta)z}^{rc})^{\sigma_{(\theta)z}^c} \left( \sum_s (\tilde{u}_z^{sc})^{1-\sigma_{(\theta)z}^{sc}} (\varrho_{(\theta)z}^{sc})^{\sigma_{(\theta)z}^{sc}} \right)^{-1}$$

where  $\tilde{w}_z^{rc}$  and  $\tilde{u}_z^c$  are appropriate measures of real wage and unemployment differentials and  $\lambda_z^c$  denotes a weighting parameter for the relative importance of these two variables in the migration decision. The parameters  $\sigma_{(\theta)z}^c$  are the elasticities by which migration flows respond to differences in the characteristics across locations (they can be skill specific) and the parameters  $\varrho_{(\theta)z}^c$  reflect further preferences across locations (which may also include policy measures, geographical/cultural distance, etc.).

We assume that the immigrants are immediately adjusting to the consumption behaviour of the host country. The number and structure of immigrants into a country then have an effect on labour markets via the unemployment term in the wage equations and via the demand effects on output.

## 4 Simulation studies

### 4.1 Weak and strong Gerschenkron effects

In this section we present three simulations to show the effects of

1. trade integration and 'weak' Gerschenkorn pattern of catching-up;
2. trade integration with 'strong' Gerschenkron pattern of catching-up;
3. the additional impact of FDI inflows with additional 'endogenous' productivity ('speeding up of technology transfer') effects.

The simulations are undertaken in a two-sector version of our model including two countries and two skill-types of workers. Country A is the technological leader and country B is the catching-up country. Sector 1 is the skill-intensive sector which also experiences faster productivity growth. In all the simulations we allow for trade in intermediate inputs, trade in investment goods and trade in consumption goods. However no transfer of rents (or international investments) across the countries is taking place. In the second scenario we allow for foreign direct investment with a high sensitivity to relative unit rents and we also introduce the endogenous productivity (speeding up of technology transfer) effect.

In the previous sections we presented the model in very general terms. In the simulations however we shall make some specific assumptions which allow a better understanding of the ongoing dynamics. In most cases we let the CES-specifications collapse to a Cobb-Douglas specification, i.e. the price elasticity equals -1 and thus nominal shares remain

invariant to changes in prices (i.e.  $\sigma \rightarrow 1$ ). First, we assume fixed coefficients in the sourcing matrix. Second, we use constant nominal shares for the demand components: Specifically we assume that 75 % of investment or consumer goods are purchased domestically and 25 % is purchased abroad. The expenditure pattern (in nominal terms) for consumption across the two sectors is assumed to be  $\alpha_k^c = 0.5$ .

In Scenario 2 we use the CES specification for the allocation of rents given in the equation above with a high sensitivity on relative rents. The other parameters can be found in table 4.1. The starting values are given in table 4.2. The starting values in all the simulations reflect a stationary state of an integrated international economy as given in table 4.2. The simulations start in this particular equilibrium and are then subject to, at first, exogenous productivity growth effects; these differ between countries (the aggregate Gerschenkron effect) and across sectors (the sectoral Gerschenkron effect).

Figure 1: Labour input coefficients

Figure 2: Rents

Figure 3: Relative price of skill intensive industries

Figure 4: Relative output

Country A succeeds in moderate labour productivity gains over time as labour input coefficients are falling to a level of 90 per cent of the starting values. We further assume that the parameter  $\gamma_{a_{ii,u}}^A$  is the same for all industries and skill-types which implies that technical progress in country A is neither sector nor factor biased.

For country B we have both the aggregate and the sectoral Gerschenkron pattern of productivity catching-up implying that the rate of catching-up is considerably higher in the sector in which the initial productivity gap is higher (sector 1); this sector is also more intensive in the use of skilled labour.<sup>10</sup> Given the structure of the starting values and the assumptions about catching-up this implies a sector-biased technical progress (but not factor-biased) in country B.

This results in a much faster decrease of the relative price of industry 1 in country B than in country A which means that country B becomes more competitive in the skill intensive sector. Due to the much faster technical progress in sector 1 per unit rents are also higher in this sector in country B. In country A (where technical progress is not biased) rents are almost equal in both sectors. They are a little bit higher in industry 1 which shows the effect of the price-equalisation process and the effect of lower input prices from country B. Unemployment in country A is even negative (meaning excess demand for labour) for both skill groups. The reason for this is that, first, technical progress (hence the labour saving effect) is quite smooth and, second, the growth process in country B creates more demand in country A (mainly for investment). As mentioned above, country B undergoes a rapid rate of labour-saving technical progress and thus undergoes a phase of transitory unemployment at the beginning. The unemployment rate

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<sup>10</sup>We distinguish between a weak and a strong Gerschenkron effect at the sectoral level: In the first case productivity growth would be higher in sector 1 simply because the initial gap is higher than in sector 2 but the convergence parameters  $\gamma_{a_{ii,u}}^c$  themselves are the same across the two sectors. The strong Gerschenkron effect implies that also the convergence parameter is higher in the sector where the initial gap is higher. In the simulations discussed we only show the runs with the strong Gerschenkron effect.

Parameter	Country A				Country B			
	Sector specific		Sector specific		Sector specific		Sector specific	
	Sector 1	Sector 2	Sector 1	Sector 2	Sector 1	Sector 2	Sector 1	Sector 2
$a_{ii}^{rr}$	0.300	0.300	0.300	0.300	0.300	0.300	0.300	0.300
$a_{ij}^{rr}$	0.075	0.075	0.075	0.075	0.075	0.075	0.075	0.075
$a_{ii}^{rs}$	0.100	0.100	0.100	0.100	0.100	0.100	0.100	0.100
$a_{ij}^{rs}$	0.025	0.025	0.025	0.025	0.025	0.025	0.025	0.025
$\pi_i$	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$\delta p_i$	0.100	0.100	0.100	0.100	0.250	0.250	0.250	0.250
$\delta \bar{p}_i$	0.010	0.010	0.010	0.010	0.150	0.150	0.150	0.150
$\kappa_{s_i}$	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$\sigma_{(\zeta)ki}$	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
$\vartheta_{(\zeta)ki}^{rrr}$	0.750	0.750	0.750	0.750	0.750	0.750	0.750	0.750
$\vartheta_{(\zeta)ki}^{rs}$	0.250	0.250	0.250	0.250	0.250	0.250	0.250	0.250
$\alpha_k$	0.500	0.500	0.500	0.500	0.500	0.500	0.500	0.500
$\sigma_\mu$	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
$\vartheta_{(\mu)ki}^{rrr}$	0.750	0.750	0.750	0.750	0.750	0.750	0.750	0.750
$\vartheta_{(\mu)ki}^{rs}$	0.250	0.250	0.250	0.250	0.250	0.250	0.250	0.250
$\sigma_\nu$	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
$\vartheta_{(\nu)ki}^{rrr}$	0.750	0.750	0.750	0.750	0.750	0.750	0.750	0.750
$\vartheta_{(\nu)ki}^{rs}$	0.250	0.250	0.250	0.250	0.250	0.250	0.250	0.250
					Sector and skill specific			
					Sector 1		Sector 2	
					Skilled	Unskilled	Skilled	Unskilled
$\bar{a}_{li,z}$	1.800	0.900	0.900	1.800	1.800	0.900	0.900	1.800
$\gamma_{\alpha_{li,z}}$	-0.015	-0.015	-0.015	-0.015	-0.015	-0.015	-0.015	-0.015
$\gamma_{(FDI)\alpha_{li,z}}$	0.000	0.000	0.000	0.000	-2.000	-2.000	-2.000	-2.000
					Economy wide, skill specific			
					Economy wide, skill specific		Economy wide, skill specific	
					Skilled	Unskilled	Skilled	Unskilled
$\delta_{h_z,IN}^C$	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
$\delta_{h_z,OUT}^C$	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$\kappa_{u_z}$	0.100	0.100	0.100	0.100	0.100	0.100	0.100	0.100
$\kappa_{w_z}$	0.010	0.010	0.010	0.010	0.010	0.010	0.010	0.010

Table 4.1: Parameter values used in simulations (Scenario 1)

Variable	Country A						Country B					
	Sector and skill specific						Sector and skill specific					
	Sector 1		Sector 2		Sector 1		Sector 2		Sector 1		Sector 2	
	Skilled	Unskilled	Skilled	Unskilled	Skilled	Unskilled	Skilled	Unskilled	Skilled	Unskilled	Skilled	Unskilled
$a_{i,z}$	2.000	1.000	1.000	2.000	8.000	4.000	2.000	4.000	2.000	4.000	2.000	4.000
$w_{i,z}$	1.000	0.500	1.000	0.500	0.500	0.100	0.500	0.100	0.500	0.100	0.500	0.100
$l_{i,z}$	2.000	1.000	1.207	2.414	6.852	3.426	2.792	3.426	2.792	3.426	2.792	5.583
	<b>Sector specific</b>						<b>Sector specific</b>					
	<b>Sector 1</b>		<b>Sector 2</b>		<b>Sector 1</b>		<b>Sector 2</b>		<b>Sector 1</b>		<b>Sector 2</b>	
$v_i$	2.500		2.000		4.400		1.400		4.400		1.400	
$p_i$	5.231		4.202		7.569		3.598		7.569		3.598	
$c_i$	5.231		4.202		7.569		3.598		7.569		3.598	
$r_i$	0.000		0.000		0.000		0.000		0.000		0.000	
$s_i$	0.000		0.000		0.000		0.000		0.000		0.000	
$j_i$	0.000		0.000		0.000		0.000		0.000		0.000	
$f_i$	0.489		0.609		0.365		0.767		0.365		0.767	
$q_i$	1.000		1.207		0.856		1.396		0.856		1.396	
	<b>Economy wide, skill specific</b>						<b>Economy wide, skill specific</b>					
	<b>Skilled</b>		<b>Unskilled</b>		<b>Skilled</b>		<b>Unskilled</b>		<b>Skilled</b>		<b>Unskilled</b>	
$l$	3.207		4.414		9.643		9.009		9.643		9.009	
$h$	3.207		4.414		9.643		9.009		9.643		9.009	
$u$	0.000		0.000		0.000		0.000		0.000		0.000	
	<b>Economy wide</b>						<b>Economy wide</b>					
$g$	0.000						0.000					

Table 4.2: Starting values used in simulations

is a little higher for the skilled workers as the rate of productivity growth is particularly high in the skill-intensive sector and the weight of this sector increases in the economy (due to substitution and trade specialisation effects). In both countries the relative output of the skill-intensive industries is rising as this industry becomes relatively cheaper. In the particular simulation selected, the relative comparative advantage moves in such a way that we observe a 'comparative advantage switchover' around period 10.

In the second scenario in which foreign direct investment flows are endogenised, these are set to be very sensitive to the differences in per-unit rents. Given our catching-up assumptions (i.e. fast unit cost reductions in the skill-intensive sector in country B) this implies very high relative unit rents in sector 1 and hence most foreign investment flows into sector 1 of country B. Next comes the additional impact of FDI on endogenous productivity growth. The result is even stronger productivity growth and cost reductions in sector 1. As a result we observe an even more dramatic improvement of the relative cost and price dynamics in favour of sector 1 and the 'switchover in comparative advantage' occurs even earlier (in period 4). There is a 'cumulative' process going on: The Gerschenkron assumption on catching-up at the sectoral level leads to an improvement in the comparative advantage position of the skill-intensive sector (the one with the higher initial gap). This is accentuated by the beneficial unit rent dynamic in favour of that sector which attracts disproportional amounts of FDI and leads to a further (endogenous) disproportionate productivity dynamics and thus pushes the comparative advantage pattern forward in time.

Figure 5: Timing of comparative advantage switchover

## 4.2 Labour market implications

The dynamics of comparative advantage has, of course, implications on the demand for different skill groups. In this model the demand for different skill groups is a function of

1. the skill composition of labour demand in the different sectors which, at any point in time, are defined by the labour input coefficients and the levels of output of the different sectors;
2. over time, changes in the skill composition result from:
  - a potential 'skill (factor) bias' in the process of technical change which might differ in different industries/sectors
  - from a sector-bias of technical change, i.e. rates of non-skill specific rates of productivity growth in different industries/sectors
  - from substitution effects due to relative wage changes (across skill groups), again the elasticities of substitution might differ across industries/sectors
  - from the evolution of output levels (driven by domestic and foreign consumption via income and price elasticities, investment and trade structures) of different sectors

As mentioned above, the scenarios presented in the previous section assumed that technical progress was neither factor nor sector biased in the lead country and - due to the weak and strong Gerschenkron effects - sector biased in the catching up country. This led to a fall in the skilled to unskilled ratio in the catching up country as technical progress was faster in the skill intensive sector. Although the structure of output shifted to the skill intensive sector the effect of the sector biased technical progress on relative employment levels of skilled and unskilled labour was stronger.

Let us now present a scenario in which technical progress is also factor biased (i.e. in favour of skilled workers) in the catching-up economy. The assumption made here is straightforward and fits naturally into a catching-up scenario: the advanced economy starts off with a technology which requires a higher skill composition of its labour force than the catching-up economy. As the catching-up process proceeds, the catching-up economy will also adjust its technology such that it ends up using the same technology as the advanced economy. This automatically induces a skill-biased technical progress in the catching-up economy (we assume no further skill bias in the advanced economy; see Fig. 6:

Figure 6: Labour input coefficients

Given this background in exogenously given paths of labour input coefficients, we shall look at two simulations which are equivalent to scenarios 1 and 2 above, i.e. scenario 3 which allows for the skill-biased pattern of technological catching-up but does not allow for FDI, while scenario 4 allows for the skill-biased pattern of technological progress but, in addition, allows both for FDI and also for the endogenous productivity (technology transfer) effect which FDI induces. The speeding up of technology transfer means that the catching-up economy moves more speedily along the given trajectories of the labour input coefficients depicted in Figure 6.

Figure 7 depicts the impact upon relative prices and relative output levels (of the two types of industries), and on relative employment levels and relative wage rates (of workers with the two types of skills) in the catching-up economy.

Figure 7: Scenarios 3 and 4

We can see that in these simulations, the relative price of the skill-intensive good falls in both scenarios. As was the case in the previous scenarios, this results from sector-biased technical progress in favour of the skill-intensive sector. However, this time, there is the additional factor-bias effect which means that there is relatively less saving of skilled labour compared to unskilled labour in both industries of the catching-up economy. This effect is stronger in the skill-intensive industry. Consequently, price competitiveness of that industry improves somewhat less than in the previous scenarios. Nonetheless, because of the sector bias in overall productivity growth, the industry nonetheless gains in competitiveness and the output structure moves in its favour. It is interesting to observe the differences between the scenario without FDI (scenario 3) and the one with endogenous FDI effects on productivity catching-up (scenario 4): we can see that the additional productivity enhancing effect of FDI leads to even faster productivity growth

in the industry in which there is more potential for catching-up (industry 1) and hence it at first improves more strongly its price competitiveness which also entails more pronounced effects on the output structure in its favour. However, as these output effects go hand in hand with a stronger demand for skilled labour in the economy (as industry 1 is also the more skill-intensive one) there is a follow-up effect on price competitiveness. Relative scarcity of skilled labour drives up the relative wage rate of skilled labour and reverses from a certain point onwards the tendency of the more skill-intensive industry to improve its price competitiveness. The impact of this relative loss in price competitiveness then shows up in a slight shift back in the output structure. Of course, a policy of sustained increases in the supply of skilled labour in the catching-up economy could counter-act this tendency.

## 5 Concluding remarks

The simulations conducted reveal the following qualitative points:

- given particular catching-up patterns, combined with wage behaviour across sectors, there is a whole spectrum of possible dynamics of comparative advantages. In particular, we can distinguish two patterns: one in which - in spite of a weak Gerschenkron/Barro pattern of catching-up which favours the industry with the higher initial productivity gap - there is an improvement in the competitiveness of the catching-up economy in the high-skill intensive sector, but there is no 'comparative advantage switchover'. In this case (Scenario 0), the catching-up economy remains (relatively) specialised in the low skill intensive branch. In the second case, we assume a 'strong' Gerschenkron pattern of catching-up in which the faster productivity growth in the skill-intensive sector stems not only from the higher initial productivity gap but also from a higher convergence parameter  $\gamma_{a_{i,z}}^c$  in this sector. In this case (Scenario 1), there is a 'comparative advantage switchover' i.e. the catching-up economy gains a specialisation advantage over the more advanced economy (which still keeps its 'absolute' productivity advantage) in the skill-intensive (higher tech) industry. As any comparative advantage in our model is purely a feature of transitory dynamic, there is a wage dynamic which over the longer time horizon erodes this comparative advantage over time (differential wage growth between skilled and unskilled workers in the catching-up economy erodes the competitive advantage of the skill intensive sector).

- The introduction of foreign direct investment opens another channel through which international integration affects output structures and specialisation in integrated economies. Rather than being directly determined by comparative (relative price) advantages, as in the case of pure trade integration, FDI flows are determined by relative unit rents. In the simulations it is shown that the dynamics of relative unit rents introduces a shift in specialisation which is related but not synonymous with the dynamic in comparative cost dynamics; hence this additional determinant of international production structures changes somewhat the extent and timing of international specialisation. This gets strengthened when we introduce an 'endogenous productivity' effect which describes the impact which FDI has on speeding up the technology transfer in the catching up economy. The 'strong

Gerschenkron effect' then gets much more pronounced and the possibility of a much faster dynamic in the up-grading process of a catching-up economy in the international division of labour arises. This feature emerged clearly in the figure on the 'timing of the comparative advantage switchover'.

- The introduction of FDI also opened up an interesting dimension in our model with regard to supply-side versus demand-side determination of production patterns.

- Lastly, the labour market implications of analysing the various channels of international integration (trade, FDI, migration) are of particular interest. While the traditional approaches to this question adopted mostly a Heckscher-Ohlin framework of analysis, the set-up of our model comes to quite different insights and conclusions to this question (see also the analysis by Feenstra and Hanson (1997), who also adopt a different framework from an Heckscher-Ohlin analysis to analyse the impact of international integration on labour markets.). The employment implications for skilled and unskilled labour are explicitly derived within a framework which takes account of the change in technology which a catching-up process entails and the potentially changing nature of comparative advantage in the course of catching-up. We show that a complex set of relationships determines the relative skill composition of the labour forces in advanced and catching-up economies.

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